

Limits

1. Compute the following limits.

$$(a) \lim_{x \rightarrow 3} \frac{x^3 - 8}{x - 2} =$$

$$(b) \lim_{x \rightarrow 2} \frac{x^3 - 8}{x - 2} =$$

$$(c) \lim_{x \rightarrow \infty} \frac{x^3 - 8}{x - 2} =$$

$$(d) \lim_{y \rightarrow \infty} \frac{5y^4 + 300y^2 - 60y + 1000}{20000 - 3y + 4y^3 - 0.01y^4} =$$

$$(e) \lim_{x \rightarrow 0} \frac{\sqrt{4+x} - 2}{x} =$$

$$(f) \lim_{t \rightarrow 2^+} \frac{t - 2}{\sqrt{t} - 2} =$$

$$(g) \lim_{x \rightarrow 0^-} \frac{x}{|x|} =$$

$$(h) \lim_{x \rightarrow 0^+} \frac{x}{|x|} =$$

Note: The last 3 limits are one-sided limits.

2. Express the following limits in terms of the variable x .

$$(a) \lim_{h \rightarrow 0} \frac{5(x+h) - 5x}{h} =$$

$$(b) \lim_{h \rightarrow 0} \frac{(x+h)^2 - x^2}{h} =$$

$$(c) \lim_{h \rightarrow 0} \frac{[2(x+h)^2 + 3(x+h)] - [2x^2 + 3x]}{h} =$$